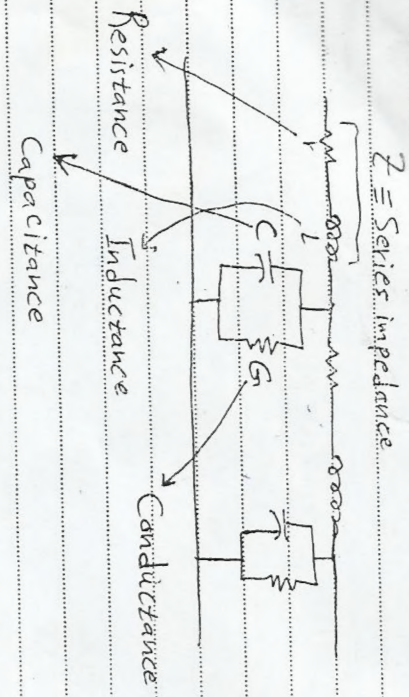


Subject: .....

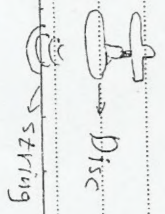
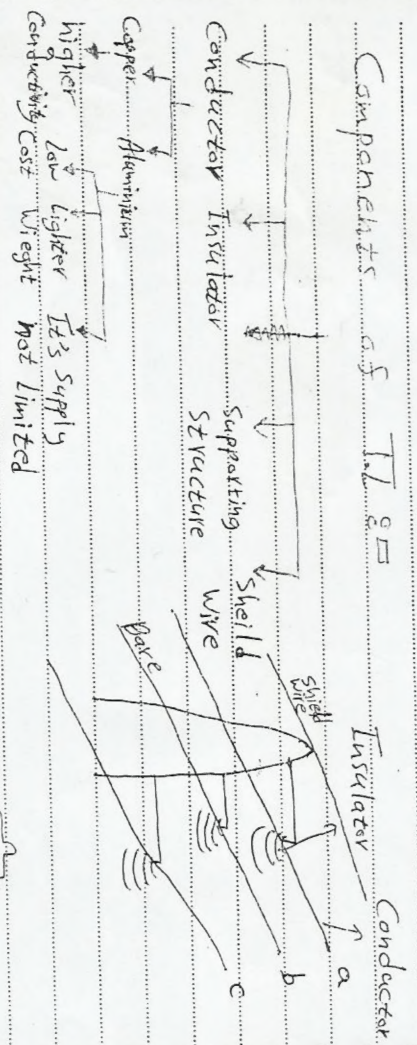
# Transmission line

Overhead T.L      Underground Cable

T.L Parameters:  $Z \equiv$  Series impedance



Comparison of T.L.  $\Rightarrow$



$$K_i = 2 \times 10^{-7} \left[ L_i L_{in} \left[ \frac{1}{r_i} \right] + \sum_{j=1}^n L_j L_{in} \left[ \frac{1}{r_{ij}} \right] \right]$$

$$a^2 + a + 1 = 0 \quad I_B = a^2 I_a \quad I_C = I_a a$$

$$a^2 \angle 240^\circ \quad a = \angle 120^\circ$$



Phase Single Conductor  
Bundle ٣

types of Aluminium

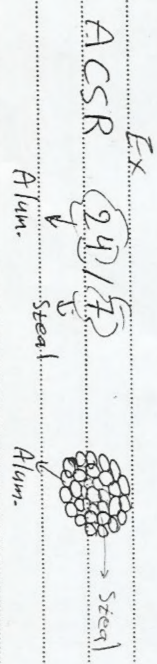
aluminum conductor steel supported (ACSS) → Use for high temperature

ACSR ≡ Alum. Conductor Steel Reinforced (most common)

AAC ≡ All Alum. Conductor (All Aluminium-Alloy Conductor)

ACAR ≡ Alum. Cond. Alloy Reinforced

Aluminum-clad Steel Conductor (Alumoweld)

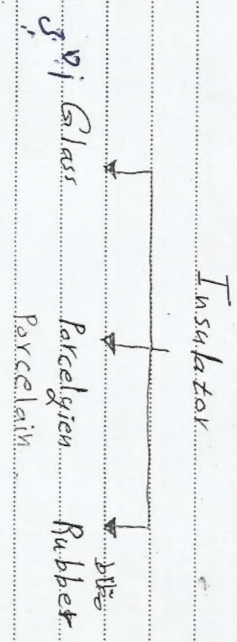
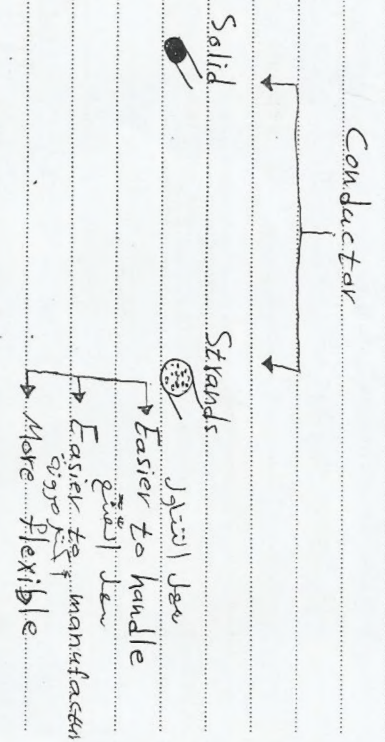


design T.L is based on optimization of electrical, mechanical, environmental and economic factors.

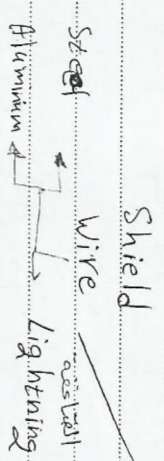
electrical factors:

- I Voltage level
- II Cond. Capacity
- III Strands
- IV Bundle

Subject: .....



« شكك البرج » Supporting Structure →



لحماية الكوابل من التلوث  
 يستخدم أيضا في الاتصالات



conductivity  $\sigma = \frac{1}{\rho}$   $\rightarrow$  resistivity

Symbol	SI Units	English Units
$\rho$	$\Omega \cdot m$	$\Omega \cdot cmil/ft$
$l$	$m$	$ft$
$A$	$m^2$	$cmil$

mil  $\times$  mil =  $mi^2$

1 mile =  $63.36 \times 10^6$  mil  
1 mile = 63360 inch

1 mile = 5280 ft

1 mile = 1760 yards

1 mile = 1609 meter

1 yard = 3 ft

1 ft = 12 inch

Circular mils

1 inch = 2.54 cm  
 $A = d^2 \text{ cmil} = \frac{\pi}{4} d^2 \text{ sq mil}$   
load = 1d

frequency ~~skin effect~~  
(skin effect)

$R_{ac} > R_{dc}$

Current density at the conductor surface  $\rightarrow$   
Current density at the center

$\rho \uparrow \leftrightarrow$  skin effect  $\uparrow$

$R_{ac} = \left( \text{factor sink effect} \right) (R_{dc})$

1 mile =  $63.36 \times 10^6$  mil = 63360 inch = 5280 ft = 1609 m

Subject:

1 mil =  $2.54 \times 10^{-8}$  Km

Resistance  $R =$

Resistivity

$\rho_T \equiv$  Conductor resistivity at temperature  $T$

$R = \frac{\rho l}{A}$   
Resistance  $\rightarrow$  length  
Cross section Area

$l \equiv$  Conductor length  
 $A \equiv$  Conductor cross-sectional Area

$R_{ac} = \frac{\rho_{ac} l}{A}$  [N]

$R_{ac} > R_{dc}$

Factors:

- I Material
- II length
- III Temperature
- IV CSA or cross section
- V Spinning (1-2) % of length [1.01]L

$R_2 = R_1 \frac{(T_2 + T_0)}{(T_1 + T_0)}$

$\uparrow$  Temp Coefficient Bundle

$\rho_{T_2} = \rho_{T_1} \left( \frac{T_2 + T_0}{T_1 + T_0} \right)$   $T_0 = 23^\circ C$



Subject: .....

mile  $\rightarrow$  mi

121

$$\rho_{50} = 10.66 \left( \frac{50 + 241.5}{(20 + 241.5)} \right)$$

$$\rho_{50} = 11.8829 \text{ } \Omega \cdot \text{cmil}/\text{ft}$$

$$R_{50} = \rho_{50} \frac{L}{A} = \frac{11.88 \times 5280 \times 10^2}{211600} = 0.3024 \text{ } \Omega/\text{mi}$$

c)

$$\text{at } 60\text{Hz} \quad \frac{R_{AC}}{R_{DC}} = \frac{0.278}{0.276} = 1.007 \quad \boxed{0.7\%}$$

$$\text{at } 60\text{Hz} \quad \frac{R_{AC}}{R_{DC}} = \frac{0.303}{0.302} = 1.003 \quad \boxed{0.3\%}$$

$$R = \frac{11.88}{211600} = 5.614 \times 10^{-5} \text{ } \Omega/\text{ft}$$

$$= 5.614 \times 10^{-5} \times 5280 = 0.296 \text{ } \Omega/\text{mi}$$

((%)) spiralling  $\rightarrow$  زيادة في المقاومة

$$0.296 + 0.296 \times \frac{2}{100} = 0.302$$

Ex 8  
A 4/d Copper Conductor with 12 Strands.  
Strand diameter is 0.1328 in. for this conductor.

a) Verify The total copper C.S.A of 211,600 cmil

b) " The dc resistance at 50°C of Assume a 2% increase in resistance due to spiralling ;  $\rho_{50} = 10.66 \text{ } \Omega \cdot \text{cmil}/\text{ft}$   $\rho_{60} = 11.88 \text{ } \Omega \cdot \text{cmil}/\text{ft}$   $T = 241.5^\circ\text{C}$

c) From Table A3 determine The percent increase in resistance at 60Hz Versus dc



$$d = 0.1328 \times 1000 = 132.8 \text{ mil}$$

$$\text{C.S.A of 1 Strand} = d^2 = (132.8)^2 = 17635.84 \text{ mil}^2$$

$$\text{C.S.A of the conductor} = 12 \times 17635.84 = 211630.08 \text{ cmil} \approx 211600 \text{ cmil}$$

$$b) \quad R_2 = R_1 \left( \frac{T_2 + T}{T_1 + T} \right)$$

$$\rho_2 = \rho_1 \left( \frac{T_2 + T}{T_1 + T} \right)$$



$H \equiv$  Magnetic field intensity  
 $B \equiv$  Magnetic flux density

$$L = L_{\text{int}} + L_{\text{ext}}$$

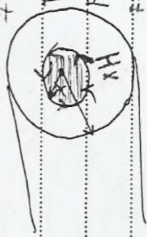
internal      external

(Constant value)  $\leftarrow L_{\text{int}} = \frac{1}{2} \chi \mu_0^{-1} H / m$

$$L_{\text{ext}} = 2 \times 10^{-7} \ln \left( \frac{D_2}{D_1} \right)$$

Assume that the conductor is sufficiently long that end effects are neglected

It is nonmagnetic  $\mu_r = 1$



It has a uniform current density (skin effect is neglected)

$$\oint H_x \cdot dl = I_x$$

$$H_x L = N I_x \quad ; \quad N = 1$$

$$2 \pi r H_x = I_x$$

$$H_x = \frac{I_x}{2 \pi r} \quad [A/m]$$

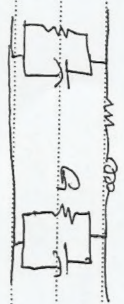
Total current  $\leftarrow$

$$\oint H_x \cdot dl = \frac{I_x}{\pi r^2} \quad \text{When uniform}$$

$$I_x = \frac{\chi^2 I}{r^2} \quad \text{When uniform current distribution within the conductor}$$

$$H_x = \frac{\chi^2 I}{2 \pi r^2} = \frac{\chi I}{2 \pi r^2}$$

Subject: .....  
 Conductance



For OHTL There are power loss due to  
 i) Leakage current at the insulators

ii) Corona: Occurs when high value of electric field strength ~~at~~ <sup>on</sup> a conductor surface causes the air to become electrically ionized and to conduct.  $\Rightarrow$  (Corona losses)

The real power loss due to corona, called Corona loss Inductance of (solid cylindrical conductor)

$$L = N \frac{d\phi}{dI} = \frac{N\phi}{I} = \frac{\lambda}{I} \quad \text{flux linkages}$$

Lenz's law  $\rightarrow$  for review  $\rightarrow L = N \frac{d\phi}{dI}$  [H]

$N=1$  (single wire)

$$L = \frac{\lambda}{I} \quad \text{Inductance}$$

$e_L = L \frac{di_L}{dt}$  [V]

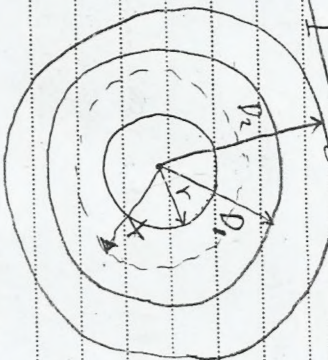


$\mu \equiv$  Permeability

Subject: ...

$\mu_0/\mu \rightarrow \mu_r = 1$  non magnetic  $\mu_r$

$$\lambda_{int} = \lambda_{int} = \frac{1}{f} \times 10^{-7} \text{ H/m}$$



$$B_x = \frac{\mu_0 I x}{2\pi x} = \frac{\mu_0 I}{2\pi x} ; I = I_x$$

$$\phi_x = B_x \cdot A$$

$$d\lambda = d\phi$$

$$d\lambda = \frac{\mu_0 I}{2\pi x} dx$$

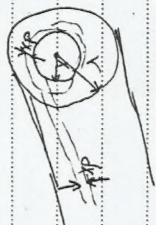
$$\lambda_{ext} = \int_0^{D_2} \frac{\mu_0 I}{2\pi x} dx$$

$$\lambda_{ext} = \frac{\mu_0 I}{2\pi} \ln\left(\frac{D_2}{D_1}\right) = 2 I \times 10^{-7} \ln\left(\frac{D_2}{D_1}\right)$$

$$\lambda_{ext} = 2 \times 10^{-7} \ln\left(\frac{D_2}{D_1}\right)$$

$$\phi = B A ; A = dx \cdot 1$$

$$d\phi = B_x dx [wb/m]$$



$$d\phi = \frac{\mu_0 I x}{2\pi r^2} dx$$

$$d\lambda_{int} = \frac{\pi r^2}{\pi r^2} d\phi$$

$$d\lambda = \frac{x^2}{r^2} \frac{\mu_0 I x}{2\pi r^2} dx$$

$$d\lambda = \frac{x^3}{2\pi r^4} \frac{\mu_0 I}{x} dx$$

$$\lambda = \int_0^r \frac{x^3}{2\pi r^4} \mu_0 I dx$$

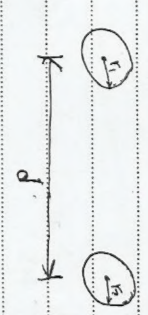
$$\lambda_{int} = \frac{\mu_0 I x^4}{8\pi r^4} \Big|_0^r = \frac{1}{2} \times 10^{-7} I [wb \cdot m]$$



Subject: .....

$L_{total} = L_{int} + L_{ext}$

Inductance of Single phase two wire line is



1<sup>st</sup> Conductor

$L_{ext} = 2 \times 10^{-7} \ln \left( \frac{D}{r_1} \right)$

$L_1 = \frac{1}{2} \times 10^{-7} + 2 \times 10^{-7} \ln \left( \frac{D}{r_1} \right)$

$L_1 = 2 \times 10^{-7} \left[ \frac{1}{2} + \ln \left( \frac{D}{r_1} \right) \right]$

$L_1 = 2 \times 10^{-7} \left[ \ln e^{\frac{1}{2}} + \ln \left( \frac{D}{r_1} \right) \right] \quad [H/m]$

$L_1 = 2 \times 10^{-7} \left[ \ln \ln \left( \frac{D e^{\frac{1}{2}}}{r_1} \right) \right]$

$L_1 = 2 \times 10^{-7} \left[ \ln \left( \frac{D}{e^{\frac{1}{2}} r_1} \right) \right]$

2<sup>nd</sup> Conductor  $L_2 = 2 \times 10^{-7} \ln \left( \frac{D}{r_2} \right)$  ;  $r_2 = e^{-\frac{1}{2}} r_1 = 0.7788 r_1$

$r_1 \equiv GMR \equiv D_s$

Geometric mean radius

## 2. Conductor

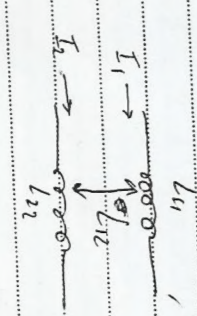
2<sup>nd</sup> conductor  $L_2 = 2 \times 10^{-7} \ln \left( \frac{D}{r_2} \right)$  ;  $r_2 = e^{-\frac{1}{2}} r_1$

Total for single phase is

2<sup>nd</sup> Single phase  $L_t = L_1 + L_2$  [H/m]

$L = 2 \times 10^{-7} \ln \left( \frac{D}{r_1} \right) + 2 \times 10^{-7} \ln \left( \frac{D}{r_2} \right)$

Flux linkage in terms of self and mutual inductances



$\lambda_1 = L_{11} I_1 + L_{12} I_2$  (mutual inductance)

2<sup>nd</sup> conductor  $\lambda_2 = L_{22} I_2 + L_{12} I_1$

$I_2 = -I_1$

$\lambda_1 = (L_{11} - L_{12}) I_1$

$\lambda_2 = (L_{22} - L_{12}) I_2$



A single phase T-L 35 km long consists of two solid round conductors each having diameter of 0.9 cm the conductor spacing is 2.5 m. Calculate the inductance per conductor and the total conductance of the single phase line.

Solution  
 $r = 0.45 \times 0.7788 \times 10^{-2} = 3.5046 \times 10^{-3} \text{ m}$

$$L = 2 \times 10^{-7} \ln \left( \frac{2.5}{3.5046 \times 10^{-3}} \right) = 1.3139 \times 10^{-6} \text{ H/m}$$

$$L = 1.3139 \times 35000 = 0.0459 \text{ H} = 45.9 \text{ mH}$$

$$L_{\text{total}} = 2L = 0.0919 \text{ H} = 91.9 \text{ mH}$$

For single phase  $L_1 = 2 \times 10^{-7} \ln \left[ \frac{D}{r_1} \right]$

$$L_{11} = 2 \times 10^{-7} \ln \left( \frac{1}{r_1} \right)$$

$$L_{12} = 2 \times 10^{-7} \ln \left( \frac{1}{r_2} \right)$$

$$L_{13} = L_{14} = -2 \times 10^{-7} \ln(D)$$

General

$$\lambda_i = L_{ii} I_i + \sum_{j=1}^N L_{ij} I_j \quad i = 1, 2, 3$$

Subst

$$\lambda_a = L_{aa} I_a + L_{ab} I_b + L_{ac} I_c$$

$$\lambda_b = L_{ba} I_a + L_{bb} I_b + L_{bc} I_c$$

Similarly

$$L_{11} = L_{11a} + L_{1ext} = 2 \times 10^{-7} \ln \left( \frac{D}{r_1} \right) = 2 \times 10^{-7} \ln \left( \frac{1}{r_1} \right) + 2 \times 10^{-7} \ln \left( \frac{D}{1} \right)$$

$$L_{12} = \frac{1}{2} \times 10^{-7}$$

$$L_{ext} = 2 \times 10^{-7} \ln \left( \frac{D}{1} \right)$$



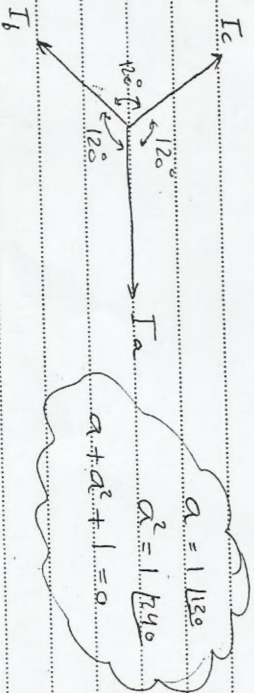
$$L_a = \frac{\lambda_a}{I_a} = \left( 2 \times 10^{-7} \ln \left( \frac{D}{r} \right) \right)$$

$$L_a = L_b = L_c = L$$

2) Asymmetrical Spacing

$$D_{12} \times D_{13} \times D_{23} \times D$$

$$\lambda_a = 2 \times 10^{-7} \left[ I_a \ln \frac{1}{r_a} + I_b \ln \left( \frac{1}{D_{12}} \right) + I_c \ln \left( \frac{1}{D_{13}} \right) \right]$$



$$I_b = a^2 I_a$$

$$I_b = I_a \angle 240^\circ$$

$$I_c = a I_a = I_a \angle 120^\circ$$

$$\lambda_a = 2 \times 10^{-7} \left[ I_a \ln \left( \frac{1}{r_a} \right) + a^2 I_a \ln \left( \frac{1}{D_{12}} \right) + a I_a \ln \left( \frac{1}{D_{13}} \right) \right]$$

$$\lambda_a = 2 \times 10^{-7} I_a \left[ \ln \left( \frac{1}{r_a} \right) + a^2 \ln \left( \frac{1}{D_{12}} \right) + a \ln \left( \frac{1}{D_{13}} \right) \right]$$

$$\lambda_i = L_{ii} I_i + \sum_{j=1}^n L_{ij} I_j \quad i \neq j$$

$$\lambda_i = 2 \times 10^{-7} \left[ I_i \ln \frac{1}{r_i} + \sum_{j=1}^n I_j \ln \frac{1}{D_{ij}} \right] \quad i \neq j$$

$$\lambda_1 = \lambda_{11} + \lambda_{12}$$

$$= L_{11} I_1 + L_{12} I_2 + L_{13} I_3$$

$$= (2 \times 10^{-7} \ln \frac{1}{r_1}) I_1 + (2 \times 10^{-7} \ln \left( \frac{1}{D_{12}} \right)) I_2$$

$$+ (2 \times 10^{-7} \ln \left( \frac{1}{D_{13}} \right)) I_3$$

Inductance of Three phase T.L

1) Symmetrical Spacing (Balancing System)  $I_a + I_b + I_c = 0$

$$D_{12} = D_{13} = D_{23} = D$$

$$\lambda_a = 2 \times 10^{-7} \left[ I_a \ln \frac{1}{r_a} + I_b \ln \frac{1}{D_{ab}} + I_c \ln \frac{1}{D_{ac}} \right]$$

$$\lambda_a = 2 \times 10^{-7} \left[ I_a \ln \left( \frac{1}{r_a} \right) + I_b \ln \left( \frac{1}{D} \right) + I_c \ln \left( \frac{1}{D} \right) \right]$$

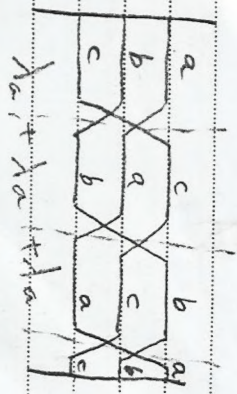
$$\lambda_a = 2 \times 10^{-7} \left[ I_a \ln \left( \frac{1}{r_a} \right) - I_a \ln \left( \frac{1}{D} \right) \right]$$

$$\lambda_a = 2 \times 10^{-7} I_a \left[ \ln \left( \frac{D}{r_a} \right) \right]$$





pose line 00



$L_a \times L_b \times L_c > 100 \text{ Km}$

$$\lambda_b + \lambda_b + \lambda_b = \lambda_b$$

$$\lambda_c + \lambda_c + \lambda_c = \lambda_c$$

multiplication

$$L_{avg} = \frac{L_a + L_b + L_c}{3}$$

$$L_{avg} = \frac{2 \times 10^{-7}}{3} \left[ 3 \ln\left(\frac{1}{f}\right) + \ln\left(\frac{1}{b_1}\right) (a + a^2) + \ln\left(\frac{1}{b_1}\right) (a + a^2) \right]$$

$$L_{avg} = 2 \times 10^{-7} \ln\left(\frac{GMD}{r}\right) ; GMD \rightarrow \sqrt[3]{D_1 D_2 D_3}$$

Subject:  $I_a = a I_b$   $I_c = a^2 I_b$   $I_a = \frac{I_b}{a^2}$  ,  $I_c = \frac{I_b}{a}$  10

$$L_a = \frac{\lambda_a}{I_a} = 2 \times 10^{-7} \left[ \ln\left(\frac{1}{f}\right) + a^2 \ln\left(\frac{1}{D_{ab}}\right) + a \ln\left(\frac{1}{D_{ac}}\right) \right]$$

$$\lambda_a \times \lambda_b \times \lambda_c$$

$$L_a \times L_b \times L_c$$

$$\lambda_b = 2 \times 10^{-7} \left[ I_b \ln\left(\frac{1}{f}\right) + I_a \ln\left(\frac{1}{D_{ba}}\right) + I_c \ln\left(\frac{1}{D_{bc}}\right) \right]$$

$$L_b = \frac{\lambda_b}{I_b} = 2 \times 10^{-7} \left[ \ln\left(\frac{1}{f}\right) + a \ln\left(\frac{1}{D_{ba}}\right) + a^2 \ln\left(\frac{1}{D_{bc}}\right) \right]$$

$$\lambda_c =$$

$$L_c = 2 \times 10^{-7} \left[ \ln\left(\frac{1}{f}\right) + a^2 \ln\left(\frac{1}{D_{ca}}\right) + a \ln\left(\frac{1}{D_{cb}}\right) \right]$$

$$I_b = a^2 I_a \quad a^2 + a + 1 = 0$$

$$I_b = I_a \quad (2^{40})$$



Subject: .....

Similarity:

$$L = 2 \times 10^{-7} \ln \left( \frac{GMD}{GMR} \right)$$

GMD  $\rightarrow$  D  $\rightarrow$  Single Phase

GMD  $\rightarrow$  D  $\rightarrow$  three Phase

GMD  $\rightarrow \sqrt{D_{12} D_{13} D_{23}} \rightarrow$  three Phase Symmetrical

GMR  $= r \rightarrow$  for all



$$\lambda_a(I) = 2 \times 10^{-7} \left[ I_a \ln \frac{1}{D_{12}} + I_b \ln \frac{1}{D_{12}} + I_c \ln \frac{1}{D_{12}} \right]$$

$$\lambda_{a(II)} = 2 \times 10^{-7} \left[ I_a \ln \frac{1}{D_{12}} + I_c \ln \frac{1}{D_{13}} + I_b \ln \frac{1}{D_{23}} \right]$$

3  $i=2$

$$\lambda_{a(III)} = 2 \times 10^{-7} \left[ I_a \ln \frac{1}{D_{12}} + I_b \ln \frac{1}{D_{13}} + I_c \ln \frac{1}{D_{23}} \right]$$

$$\lambda_{a(III)} = \frac{\lambda_{a(I)} + \lambda_{a(II)} + \lambda_{a(III)}}{3}$$

$$\lambda_a = 2 \times 10^{-7} I_a \ln \frac{GMD}{r}$$

$$GMD = \sqrt[3]{D_{12} D_{13} D_{23}}$$

$$L_a = \frac{\lambda_a}{I_a} = 2 \times 10^{-7} \ln \frac{GMD}{GMR}$$

Ex 2

A single circuit, three phase transposed line operated at 60 Hz is arranged as shown.

The conductors are ACSR Drake, Find the inductive reactance per mile per phase.





Subject: .....

→ feet  
→ inch

1 1 12

distance of Composite Conductor lines =



Conductor X Conductor Y



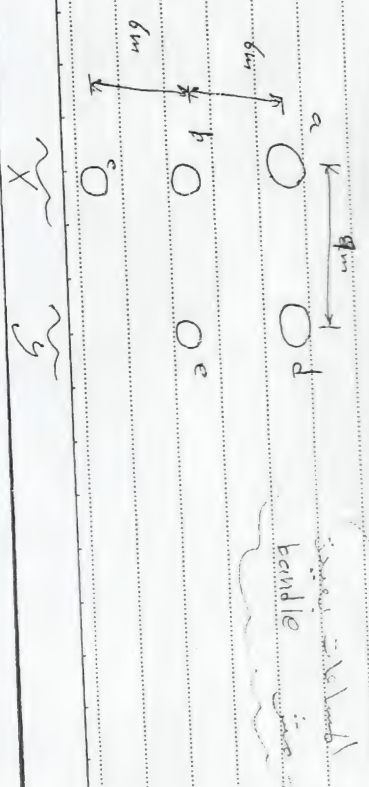
$$L_x = 2 \times 10^{-7} \ln \left( \frac{D_{xy}}{D_{sx}} \right) \rightarrow \text{mutual Geometric Mean Distance}$$

$$L_y = 2 \times 10^{-7} \ln \left( \frac{D_{xy}}{D_{sy}} \right)$$

### Example 2

One circuit of a single phase TL is composed of three solid 0.25 cm radius wires. The return circuit is composed of two 0.5 cm radius wires. Find the inductance due to each current in each side of the line & the inductance of the complete line in henry per meter & in mH/mi

Note



### Solution

$$X_L = \omega L$$

$$L = 2 \times 10^{-7} \ln \left( \frac{GMD}{GMR} \right)$$

$$GMD = \sqrt{(20)(20)(38)} = 24.8 \text{ ft}$$

$$GMR = r = D_s = 0.0375 \text{ ft}$$

$$L = 2 \times 10^{-7} \ln \left( \frac{24.8}{0.0375} \right) = 13 \times 10^{-7} \text{ H/m}$$

$$X_L = 2 \pi (60) \times 13 \times 10^{-7} = 4.9 \times 10^{-4} \Omega/\text{m}$$

$$1 \text{ mile} = 1609 \text{ m}$$

$$X_L = 4.9 \times 10^{-4} \times 1609 = 0.788 \Omega/\text{mi}$$



Solution

$$D_g = \sqrt[3]{D_g \times D_{de} \times D_{ed}} = 0.153 \text{ m}$$

$$L_g = 2 \times 10^{-7} \ln \left( \frac{10.744}{0.153} \right) = 8.503 \times 10^{-7} \text{ H/m}$$

$$L_{tot} = L_x + L_g = 14.715 \times 10^{-7} \text{ H/m}$$

$$L_{tot} = 14.715 \times 10^{-7} \times 1609 = 2.37 \text{ mH/mi}$$

### GMR of Bundled conductors

- 1) Improve the line performance
- 2) Increases power capability of the line
- 3) Reduces Corona losses

$$D_s = \sqrt[3]{D_a \times D_b \times D_c}$$

$$D_s = 0.0$$

$$D_s = \sqrt[3]{D_a \times D_b \times D_c} = \sqrt[3]{D_s}$$

$$D_s = \sqrt[3]{D_s \times D_s \times D_s} = \sqrt[3]{D_s^3}$$

في الحل 3 في 7788  
في الحل 3 في 7788  
في الحل 3 في 7788

$$D_s = r$$

$$r = 10.744$$

$$L_x = 2 \times 10^{-7} \ln \left( \frac{D_m}{D_x} \right)$$

$$D_m = \sqrt[3]{D_a D_b D_c} = 10.743 \text{ m}$$

$$D_m = 10.743 \text{ m}$$

$$D_{ce} = \sqrt[3]{D_a D_b D_c} = 10.743 \text{ m}$$

$$D_{sx} = \sqrt[3]{D_a \times D_b \times D_c \times D_{ce} \times D_{de} \times D_{ed} \times D_{ee} \times D_{dd} \times D_{dc} \times D_{cb} \times D_{ba} \times D_{aa}} = 1.944$$

$$D_s = \text{GMR} = r$$

$$D_s = 0.25 \times 0.7788 \times 10^{-7} = 1.944$$

$$D_{sx} = 1.944$$

$$D_{sx} = 0.481 \text{ m}$$

$$L_x = 2 \times 10^{-7} \ln \left( \frac{10.743}{0.481} \right) = 6.212 \times 10^{-7} \text{ H/m}$$



Figure of Three phase double circuit line

a o o e  
b o o b  
c o o c



$l_a = l_b = l_c$

$$GMD = \sqrt[3]{D_{AB} \times D_{BC} \times D_{AC}}$$

$$D_{AB} = \sqrt[4]{D_{Ab} \times D_{Ab} \times D_{Ab} \times D_{Ab}}$$

$$D_{BC} = \sqrt[4]{D_{Bc} \times D_{Bc} \times D_{Bc} \times D_{Bc}}$$

$$D_{AC} = \sqrt[4]{D_{Ac} \times D_{Ac} \times D_{Ac} \times D_{Ac}}$$

$$D_{SA} = \sqrt[4]{D_{SaA} \times D_{SaA} \times D_{SaA} \times D_{SaA}} = \sqrt{D_s D_{aA}}$$

$$D_{SB} = \sqrt[4]{D_{SbA} \times D_{SbA} \times D_{SbA} \times D_{SbA}} = \sqrt{D_s D_{bA}}$$

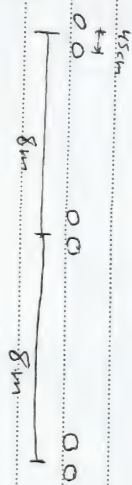
$$D_{SC} = \sqrt[4]{D_{ScA} \times D_{ScA} \times D_{ScA} \times D_{ScA}} = \sqrt{D_s D_{cA}}$$

$$GMR = \sqrt[3]{D_{SA} \times D_{SB} \times D_{SC}}$$

Subject:

$$D_s = \sqrt[4]{(R \sqrt{2} l)^4} = 1.094 \sqrt{D_s l^3}$$

Ex 2



ACSR Pheasant

$$X_L = ? \text{ } [\Omega / \text{km}]$$

$$GMD = \sqrt[3]{8 \times 16 \times 8} = 18.0794 \text{ m}$$

~~GMR~~

from Table  $D_s$  for phase = 0.0142 m

$$f_{\text{band}} = D_s^b = \sqrt{R d} = \sqrt{(0.0142)(0.95)} = 0.0799 \text{ m}$$

$$L = 2 \times 10^{-2} \ln \left( \frac{GMD}{GMR} \right) = 9.67 \times 10^{-7} \text{ H/m}$$

$$L = 9.67 \times 10^{-4} \text{ H/km}$$

$$X_L = 2\pi(60)(L) = 0.3647 \text{ } \Omega / \text{km}$$



Capacitance

Capacitance is  
a function of  
the amount of capacitance between  
conductors.

is a function of  $\omega$

Stephen J. Laury, David Sand, Keith

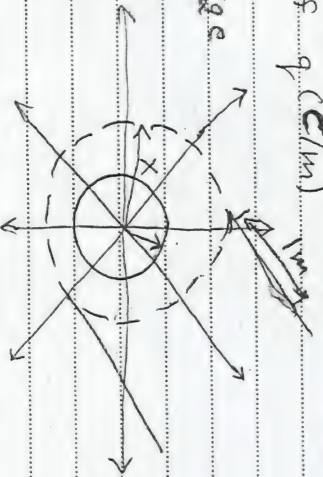
Candidate Size.....

Spacing between Conductors

height above ground.

Consider a long cylindrical conductor with radius  $r$  carrying a charge of  $q$  (C/m).

flux charge

$$\epsilon = 0$$


The charge on conductor gives rise to an electric field with radial flux lines.

\* The total electric flux is numerically equals the value of charge on conductor.

.....

Christy 10

2  
4  
1  
0  
0  
A,

2000

c o o o a

Dr. S. J. Hall

St. Paul & Northern Pacific

1884

$$D_5 = \sqrt{D_4 \times d}$$

$$P_{SA} = \sqrt{P_S P_{\text{act}}}$$

$$D_{SB} = \sqrt{D_5^b D_{bb}}$$

25

21 Dec 19

Glacier

.....



Gauss's Law :

$$D = \frac{q}{A} \quad C = \frac{Q}{V}$$

electric field density

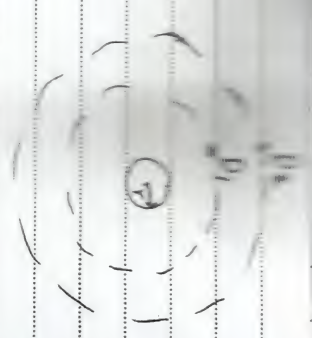
$$D = \frac{q}{2\pi \times (l)} = \frac{q}{2\pi \times r \times l} = \frac{q}{2\pi \times r}$$

$E = \frac{D}{\epsilon}$   
electric field intensity  $\epsilon \rightarrow$  Permittivity  $\epsilon_0 \epsilon_r$

$$E = \frac{q}{2\pi \times r \times \epsilon_0}$$

The potential difference between cylinders from position  $D_1$  to  $D_2$  is defined as the work done in moving a unit charge of 1 Coulomb from  $D_2$  to  $D_1$ . Through the electric field produced by the charge on conductor.

$$V_{12} = \int_{D_1}^{D_2} E \, dx$$



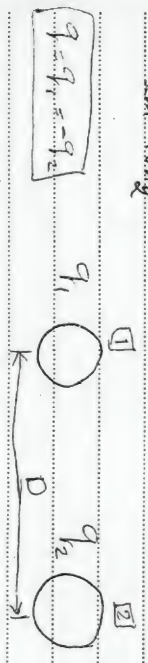
$$V_{12} = \int_{D_1}^{D_2} \frac{q}{2\pi \epsilon_0 \times r} \, dx = \frac{q}{2\pi \epsilon_0} \ln\left(\frac{D_2}{D_1}\right) \quad [V/m]$$

$$Q = q \times L \quad [Coulomb]$$

$\downarrow$   
C/m

Capacitance of a single phase lines

Single phase line consisting of 2 conductors with 1m long



\* Assuming cond. ① is alone

$$V_{12}(q_1) = \frac{q_1}{2\pi \epsilon_0} \ln\left(\frac{D}{r}\right)$$



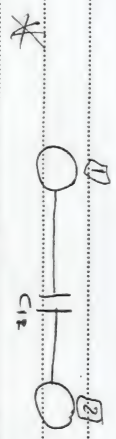
$$V_{12} = \frac{q}{2\pi\epsilon_0} \ln\left(\frac{D}{r}\right) - \frac{q}{2\pi\epsilon_0} \ln\left(\frac{r}{D}\right)$$

$$V_{12} = \frac{q}{2\pi\epsilon_0} \left[ \ln\left(\frac{D}{r}\right)^2 \right] = \frac{q}{\pi\epsilon_0} \ln\left(\frac{D}{r}\right)$$

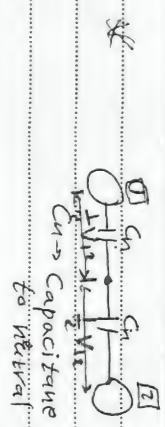
for single phase

$$V_{12} = \frac{q}{\pi\epsilon_0} \ln\left(\frac{D}{r}\right) \quad [V/m]$$

$$C_{12} = \frac{q}{V_{12}} = \frac{\pi\epsilon_0}{\ln(D/r)} \quad [F/m]$$



$C_{12} \rightarrow$  line to line capacitance



$$C_n = \frac{2\pi\epsilon_0}{\ln(D/r)} \quad [F/m]$$

$$C_{12} = \frac{C_n^2}{2C_n} = \frac{C_n}{2}$$

$$C_n = 2 C_{12} \quad [F/m]$$

$$C_n = 0.0556 \frac{\mu F}{km} \ln\left(\frac{D}{r}\right)$$

\* Assuming cond. ② is alone

$$V_{12}(q_1) = \frac{q_2}{2\pi\epsilon_0} \ln\left(\frac{D}{r}\right)$$

$$\therefore V_{12}(q_1) = -V_{12}(q_2)$$

$$V_{12}(q_1) = \frac{q_2}{2\pi\epsilon_0} \ln\left(\frac{r}{D}\right)$$

$$V_{12} = V_{12}(q_1) + V_{12}(q_2)$$

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~~Handwritten scribbles.~~

$$V_{12} = \frac{q_1}{2\pi\epsilon_0} \ln\left(\frac{D}{r}\right) + \frac{q_2}{2\pi\epsilon_0} \ln\left(\frac{r}{D}\right)$$

$$q_1 = -q_2 = q$$



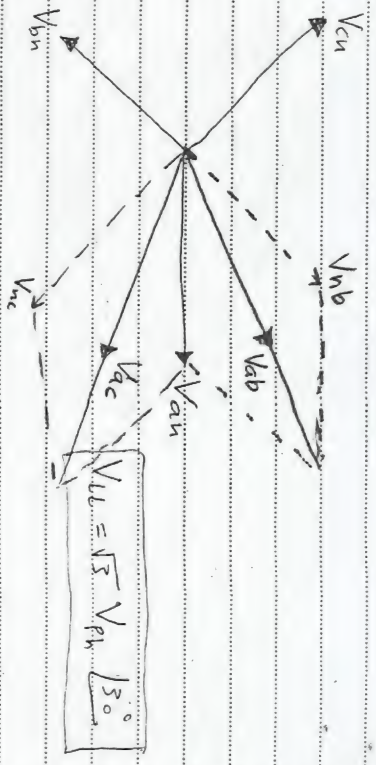
$$\epsilon_0 \ln \left( \frac{D}{r} \right) + q_b \ln \left( \frac{D}{r} \right) + q_c \ln \left( \frac{D}{r} \right)$$

$$V_{ac} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln \left( \frac{D}{r} \right) + q_b \ln \left( \frac{D}{r} \right) + q_c \ln \left( \frac{D}{r} \right) \right]$$

$$V_{ab} + V_{bc} = \frac{1}{2\pi\epsilon_0} \left[ 2q_a \ln \left( \frac{D}{r} \right) - q_a \ln \left( \frac{D}{r} \right) \right]$$

$$= \frac{1}{2\pi\epsilon_0} \left[ 2q_a \ln \left( \frac{D}{r} \right) + q_a \ln \left( \frac{D}{r} \right) \right]$$

$$V_{ab} + V_{bc} = \frac{3}{2\pi\epsilon_0} q_a \ln \left( \frac{D}{r} \right)$$



$$V_{ab} = V_{an} + V_{bn} = \sqrt{3} V_{an} \angle 30^\circ = \sqrt{3} V_{an} \left[ \cos 30^\circ + j \sin 30^\circ \right]$$

$$V_{ac} = V_{an} + V_{cn} = \sqrt{3} V_{an} \angle -30^\circ = \sqrt{3} V_{an} \left[ \cos 30^\circ - j \sin 30^\circ \right]$$

$$V_{ab} + V_{ac} = 3V_{an}$$

Subject: .....

Potential Difference in a multi-conductor Configuration

$$V_{ij} = \frac{1}{2\pi\epsilon_0} \sum_{k=1}^n q_k \ln \left( \frac{D_{ik}}{D_{jk}} \right)$$

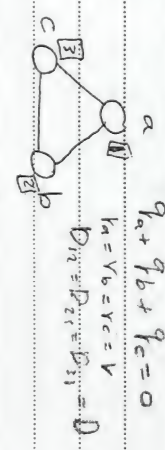
for three phase

$$V_1 = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln \left( \frac{D_{12}}{D_{11}} \right) + q_b \ln \left( \frac{D_{12}}{D_{11}} \right) + q_c \ln \left( \frac{D_{12}}{D_{11}} \right) \right]$$

Capacitance of 3-phase transmission lines

1 Symmetrical Spacing

$$V_{ab} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln \left( \frac{D_{12}}{D_{11}} \right) + q_b \ln \left( \frac{D_{12}}{D_{11}} \right) + q_c \ln \left( \frac{D_{12}}{D_{11}} \right) \right]$$



$$+ q_b \ln \left( \frac{D_{12}}{D_{11}} \right) + q_c \ln \left( \frac{D_{12}}{D_{11}} \right)$$

$$V_{ab} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln \left( \frac{D_{12}}{D_{11}} \right) + q_b \ln \left( \frac{D_{12}}{D_{11}} \right) + q_c \ln \left( \frac{D_{12}}{D_{11}} \right) \right]$$



$$V_{avg} = \frac{V_{ab(I)} + V_{ab(II)} + V_{ab(III)}}{3}$$

$$G_{MD} = \sqrt{D_1 D_2 D_3} \cdot \rho_{03}$$

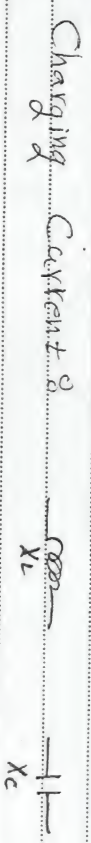
$$V_{ab(ave)} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln\left(\frac{G_{MD}}{r}\right) + q_b \ln\left(\frac{r}{G_{MD}}\right) \right]$$

Similar

$$V_{ac} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln\left(\frac{G_{MD}}{r}\right) + q_c \ln\left(\frac{r}{G_{MD}}\right) \right]$$

$$V_{ab} + V_{ac} = \frac{3q_a}{2\pi\epsilon_0} \ln\left(\frac{G_{MD}}{r}\right)$$

$$C_{an} = \frac{2\pi\epsilon_0}{\ln\left(\frac{G_{MD}}{r}\right)}$$



$V = I W$  for single phase line

$$I_{cn} = I W C_n V_{an}$$

phase to neutral voltage

Capacitance to neutral

$$C_{an} = \frac{q_a}{V_{an}} = \frac{2\pi\epsilon_0}{\ln\left(\frac{D}{r}\right)} \quad f/m$$

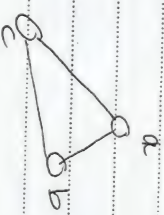
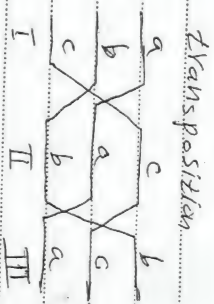
$$3V_{an} = \frac{3q_a \ln\left(\frac{D}{r}\right)}{2\pi\epsilon_0}$$

$$C_{an} = 0.0556$$

$$\ln\left(\frac{D}{r}\right)$$

$\mu F/km$

8 A symmetrical Spacing:



$$V_{ab(II)} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln\left(\frac{D_2}{r}\right) + q_b \ln\left(\frac{r}{D_2}\right) + q_c \ln\left(\frac{D_2}{D_1}\right) \right]$$

$$V_{ab(II)} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln\left(\frac{D_2}{r}\right) + q_b \ln\left(\frac{r}{D_2}\right) + q_c \ln\left(\frac{D_2}{D_1}\right) \right]$$

$$V_{ab(II)} = \frac{1}{2\pi\epsilon_0} \left[ q_a \ln\left(\frac{D_1}{r}\right) + q_b \ln\left(\frac{r}{D_1}\right) + q_c \ln\left(\frac{D_1}{D_2}\right) \right]$$



# Effects of Bundling

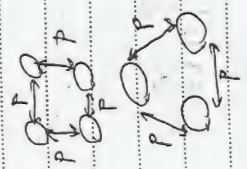
$$C_n = 2\pi \epsilon_0 \ln\left(\frac{GMD}{r_b}\right)$$

$$r_b = \sqrt[3]{r \times d}$$

$$r_b = \sqrt[3]{r \times d}$$

$$r_b = \sqrt[3]{r \times d^2}$$

$$r_b = 1.09 \sqrt[3]{r \times d^3}$$



Capacitance of Three phase double circuit lines

$$C_n = \frac{2\pi \epsilon_0}{\ln\left(\frac{GMD}{GMR_c}\right)}$$



$$GMR_c = \sqrt[3]{Z_A \times Z_B \times Z_C}$$

$$Z_A = \sqrt{r \times D_{aa}}$$

$$Z_B = \sqrt{r \times D_{bb}}$$

$$Z_C = \sqrt{r \times D_{cc}}$$

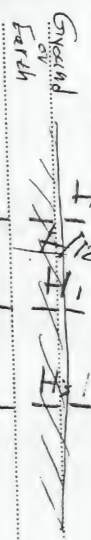
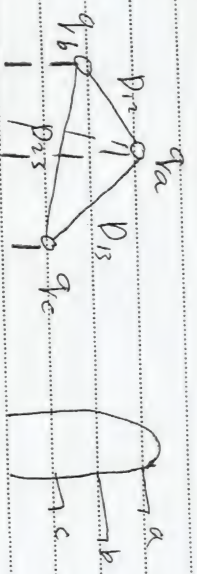
$$GMD = \sqrt[3]{D_{AB} \times D_{BC} \times D_{AC}}$$

Similar to inductance

of earth on the capacitance of it  
 $L_g =$

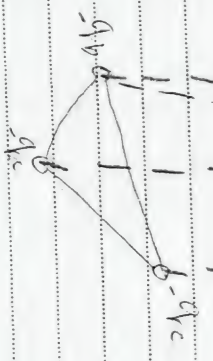
Assuming That The earth is perfect conductor in the form of the horizontal plane of infinite extent.

$$V_{ab} = \frac{1}{2\pi \epsilon_0} \left[ q_a \left[ \ln\left(\frac{D_{12}}{r}\right) - \ln\left(\frac{H_{12}}{H_1}\right) \right] + q_b \left[ \ln\left(\frac{D_{13}}{r}\right) - \ln\left(\frac{H_{13}}{H_1}\right) \right] + q_c \left[ \ln\left(\frac{D_{23}}{r}\right) - \ln\left(\frac{H_{23}}{H_1}\right) \right] \right]$$



$$C_n = \frac{2\pi \epsilon_0}{\ln\left(\frac{GMD}{r}\right) - \ln\left(\frac{H_1 H_2 H_3}{H_1 H_2 H_3}\right)}$$

\* The effect of earth is to increase the capacitance of the line.





Subject:.....

The use of table in Inductive reactance 21

ind the inductive inductive reactance of a single phase line operating at 60 Hz. The Cond. is parallel and spacing is 25 ft.

Solution

for  $L = 2 \times 10^{-7} \ln \left( \frac{GMD}{GMR} \right) = 2 \times 10^{-7} \ln \left( \frac{20}{0.0217} \right)$  Conductor

$L = 1.36 \times 10^{-6} \text{ H/m}$

for Single phase  $L = 2 \times L_{\text{for Conductor}}$

$L = 2.73 \times 10^{-3} \text{ H/m}$

$X_L = 166589 \Omega/\text{mi}$

Other way

from A3  $X_a = 0.465 \Omega/\text{mi}$  table

from A4  $X_d = 0.3635 \Omega/\text{mi}$  table

for Conductor  $X_L = X_a + X_d = 0.8285 \Omega/\text{mi}$

for Single phase  $X_L = 1.657 \Omega/\text{mi}$

$X_L = \omega L = 2\pi f L = 2\pi \times 60 \times 10^{-3} \ln \left( \frac{GMD}{GMR} \right)$

$X_L = 4\pi f \times 10^{-3} \ln \left( \frac{GMD}{GMR} \right) \Omega/\text{m}$

$X_L = 2.022 \times 10^{-3} f \ln \left( \frac{GMD}{GMR} \right) \Omega/\text{mi}$

$X_L = (2.022 \times 10^{-3} f \ln \left( \frac{1}{GMR} \right) + 2.022 \times 10^{-3} f \ln(GMD))$

$\ln(GMD)$

$X_a \triangleq$  Inductive reactance at 1 ft spacing

$X_d \triangleq$  " " Spacing factor







E For the bandel cond. Line shown in Fig each is ACSR 1.270.000 cmil Pheasant Find

a → The inductance of the Line in mH/Km/ph and The inductive reactance

b → The series impedance in  $\Omega/\text{mi}/\text{ph}$

c → The capacitance of the Line in  $\mu\text{F}/\text{Km}/\text{ph}$  and total capacitive reactance at 60Hz if the Line is 120 Km

d → The charging current per Km if operating Voltage 220KV



solution (a)

Bandel, ACSR,

اولاً مش عايز دايستراو ال رازامنه جدول

From the table

$$D_s = GMR_o = 0.0466 \text{ Ft}$$

للبندل الواحد فقط للسندل كوندكتور

$$L = 2 \times 10^{-7} \ln \frac{GMR_x}{GMD}$$

لما أنفا ثري فيز

$$GMD = \sqrt[3]{8816} = 10.08 \text{ m}$$

$$GMR_x = \sqrt{D_s d} = 0.0466 \times 0.025 = 0.025$$

$$= \sqrt{0.45 \left( \frac{0.0466 \times 12 \times 2.54}{2.54} \right)} = 0.0799 \text{ m}$$

$$L = 2 \times 10^{-7} \ln \left( \frac{10.08}{0.0799} \right) = 0.967 \times 10^{-6} \text{ H/m}$$



$$X_L = \omega L = 2\pi \times 60 \times 0.967 \times 10^{-6} = \boxed{\phantom{00}} \Omega/m$$

$$= \boxed{\phantom{00}} \times 1000 \Omega/Km \quad 0.365 \Omega/Km$$

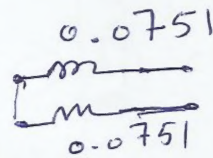
[b] series impedance  $Z = R + jX_L$

$$X_L = 0.365 \times 1.609 = 0.587 \Omega/mi$$

بالنسبة الى طول خط

$$R_{20\%} = 0.0751 \Omega/mi$$

$$Z = \frac{0.0751}{2} + 0.587$$



if Bandel (3)  $\dots \sqrt[3]{D_s d^2}$

$$\frac{R}{3}$$

i Bandel (4)  $\dots \sqrt[4]{D_s d^3}$

$$\frac{R}{4}$$

[c]

$$C = \frac{2\pi \epsilon_0}{\ln\left(\frac{GMR}{r^b}\right)} \quad \text{bandel}$$

نصف قطر  
 $r = \frac{\text{diam}}{2}$

$$r^b = \sqrt{r d} =$$

$$r^b = \frac{1.382}{2} \text{ inch} = \frac{0.691 \times 2.54}{100} = 0.0176m$$

$$r^b = \sqrt{0.0176 \times 0.45} = 0.089$$

$$C = \frac{2\pi \times 8.85 \times 10^{-12}}{\ln\left(\frac{10.08}{0.089}\right)} = 11.75 \times 10^{-12} \text{ F/m}$$

$$X_C = \frac{1}{\omega C} = \frac{1}{2\pi \times 60 \times 11.75 \times 10^{-12}} = \boxed{\phantom{00}} \Omega/m$$

$$\frac{225.866 \times 10^6}{120 \times 10^3} = 1882$$

$$C_T = 0.01175 \times 120 = 1.409 \mu F$$

$$X_C = \frac{1}{\omega C_T} = 1883$$

$$\omega = 2\pi f_c$$

[2]

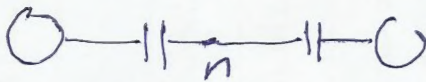
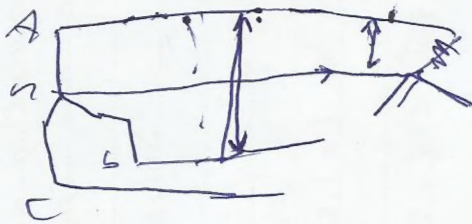


(D)  $I_{ch} = \omega C_n V_{an}$

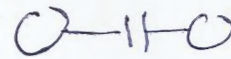
$= \omega (2 \times 60 \times 11.76 \times 10^{-12}) \times \frac{220 \times 10^3}{\sqrt{3}} = 0.563 \text{ A/m}$

$0.563 \text{ A/Km}$

Line voltage to Phase



$\frac{2 \pi \epsilon_0}{\ln(1)}$



$\frac{\pi \epsilon_0}{\ln(1)}$

(E) total reactive power of the Line

$Q_{3ph} = \sqrt{3} \frac{V I}{\text{LL}} = \sqrt{3} 220 \times 10^3 \times 0.563 =$

if one phase  $Q_{1\phi} = V_{ph} I$